

TABLE 1. Important Continuous Random Variables (Families)

	$\Theta$	$f_X(x)$	$m_X$	$\sigma_X^2$	$\Phi_X(\omega)$
Uniform( $a, b$ )	$\mathbb{R}^2$	$\frac{1}{b-a} \mathbb{1}(a < x < b)$	$\frac{a+b}{2}$	$\frac{(b-a)^2}{12}$	$\frac{e^{i\omega b} - e^{i\omega a}}{i\omega(b-a)}$
Exponential( $\lambda$ )	$\mathbb{R}_+$	$\frac{1}{\lambda} e^{-\frac{x}{\lambda}} \mathbb{1}(x > 0)$	$\lambda$	$\lambda^2$	$\frac{\lambda}{\lambda - i\omega}$
Gaussian( $\mu, \sigma^2$ )	$\mathbb{R} \times \mathbb{R}_+$	$\frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$	$\mu$	$\sigma^2$	$e^{i\mu\omega - \frac{\sigma^2}{2}\omega^2}$
Cauchy( $\mu, \sigma$ )	$\mathbb{R} \times \mathbb{R}_+$	$\frac{1}{\pi\sigma(1+(\frac{x-\mu}{\sigma})^2)}$	N/A	N/A	$e^{-\alpha \omega  + i\mu\omega}$
Gamma( $\alpha, \beta$ )	$\mathbb{R}_+ \times \mathbb{R}_+$	$\frac{x^{\alpha-1} e^{-\frac{x}{\beta}}}{\Gamma(\alpha)\beta^\alpha} \mathbb{1}(x > 0)$	$\alpha\beta$	$\alpha\beta^2$	$\frac{1}{(1-i\omega\beta)^\alpha}$
Chi-Squared( $k$ )	$\mathbb{Z}_+$	$\frac{x^{\frac{k}{2}-1} e^{-\frac{x}{2}}}{\Gamma(\frac{k}{2})2^{\frac{k}{2}}} \mathbb{1}(x > 0)$	$k$	$2k$	$\frac{1}{(1-2i\omega)^{\frac{k}{2}}}$
Beta( $\alpha, \beta$ )	$\mathbb{R}_+ \times \mathbb{R}_+$	$\frac{\Gamma(\alpha+\beta)}{\Gamma(\alpha)\Gamma(\beta)} x^{\alpha-1} (1-x)^{\beta-1} \mathbb{1}(0 < x < 1)$	$\frac{\alpha}{\alpha+\beta}$	$\frac{\alpha\beta}{(\alpha+\beta)^2(\alpha+\beta+1)}$	
Laplacian( $\alpha$ )	$\mathbb{R}_+$	$\frac{\alpha}{2} e^{-\alpha x }$	0	$\frac{2}{\alpha^2}$	$\frac{\alpha^2}{\omega^2 + \alpha^2}$
Rayleigh( $\alpha$ )	$\mathbb{R}_+$	$\frac{x}{\alpha^2} e^{-\frac{x^2}{2\alpha^2}} \mathbb{1}(x > 0)$	$\sqrt{\frac{\pi}{2}}\alpha$	$(2 - \frac{\pi}{2})\alpha^2$	
Pareto( $x_m, \alpha$ )	$\mathbb{R}_+ \times \mathbb{R}_+$	$\frac{\alpha x_m^\alpha}{x^{\alpha+1}} \mathbb{1}(x > x_m)$	$\frac{\alpha x_m}{\alpha-1} \ (\alpha > 1)$	$\frac{\alpha x_m^2}{(\alpha-2)(\alpha-1)^2} \ (\alpha > 2)$	
Lognormal( $\mu, \sigma^2$ )	$\mathbb{R} \times \mathbb{R}_+$	$\frac{1}{\sqrt{2\pi\sigma^2}} \frac{1}{x} e^{-\frac{(\log x - \mu)^2}{2\sigma^2}}$	$e^{\mu + \frac{\sigma^2}{2}}$	$e^{2(\mu + \sigma^2)} - e^{2\mu + \sigma^2}$	
Double Exponential( $\mu, \sigma$ )	$\mathbb{R} \times \mathbb{R}_+$	$\frac{1}{2\sigma} e^{-\frac{ x-\mu }{\sigma}}$	$\mu$	$2\sigma^2$	

See Leon-Garcia, P164.